# Bayesian Principles for Learning-Machines

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# Al that learn like humans

Learn and adapt quickly throughout their lives

# Human Learning at the age of 6 months.



# Converged at the age of 12 months



Transfer skills at the age of 14 months



### **Bayesian Principles**

### **Human learning**

Life-long learning from small chunks of data in a non-stationary world Bulk learning from a large amount of data in a stationary world

**Deep learning** 

This talk

#### My current research focuses on reducing this gap!

Parisi, German I., et al. "Continual lifelong learning with neural networks: A review." *Neural Networks* (2019)
Geisler, W. S., and Randy L. D. "Bayesian natural selection and the evolution of perceptual systems." *Philosophical Transactions of the Royal Society of London. Biological Sciences* (2002)

### Bayesian (Principles for) Learning Machines

- Uncertainty
  - What you don't know now, can hurt you later
- Learning
  - Derive learning-algorithms from Bayes
- Knowledge
  - Extract knowledge as memorable examples

# Which is a good classifier?



# Which is a good classifier?



# **Uncertainty of Deep Nets**



One Model vs Many.

A key idea in Bayes is to estimate distributions over model parameters (e.g., Gaussian).

Khan, et al. "Fast and scalable Bayesian deep learning by weight-perturbation in Adam." *ICML* (2018).
Osawa et al. "Practical Deep Learning with Bayesian Principles." NeurIPS (2019).

## **Image Segmentation**

Image



True Segments



Prediction



Uncertainty





Kendall, Alex, Yarin Gal, and Roberto Cipolla. "Multi-task learning using uncertainty to weigh losses for scene geometry and semantics." *CVPR*. 2018.

# **Reduce Overfitting**

### Standard DL

### **Bayesian DL**





Left figure is cross-validation. Right figure is "Marginal Likelihoods".

### Bayesian (Principles for) Learning Machines

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# Bayesian Learning Rule $\min_{\theta} \ell(\theta) \quad \text{vs} \quad \min_{q \in \mathcal{Q}} \mathbb{E}_{q(\theta)}[\ell(\theta)] - \mathcal{H}(q)$ Exponential-family Approx.

Deep Learning algo:  $\theta \leftarrow \theta - \rho H_{\theta}^{-1} \nabla_{\theta} \ell(\theta)$ Bayes learning rule:  $\lambda \leftarrow \lambda - \rho \nabla_{\mu} \left( \mathbb{E}_{q}[\ell(\theta)] - \mathcal{H}(q) \right)$  $\uparrow \qquad \uparrow \qquad \land \text{Natural Gradient}$ Natural and Expectation parameters of an exponential family distribution q

#### By changing *Q*, we can recover DL algorithms (and more)

- 1. Khan and Lin. "Conjugate-computation variational inference: Converting variational inference in nonconjugate models to inferences in conjugate models." Alstats (2017).
- 2. Khan and Rue. "Learning-Algorithms from Bayesian Principles" (2020) (work in progress, an early draft available at <a href="https://emtiyaz.github.io/papers/learning\_from\_bayes.pdf">https://emtiyaz.github.io/papers/learning\_from\_bayes.pdf</a>)

### **Bayesian learning rule:** $\lambda \leftarrow \lambda - \rho \nabla_{\mu} (\mathbb{E}_q[\ell(\theta)] - \mathcal{H}(q))$

Learning Algorithm	Posterior Approx.	Algorithmic Approx.	Sec.
Optimization Algorithms			
Gradient Descent	Gaussian (fixed cov.)	Delta approx.	1.4
Newton's method	Gaussian	"	1.4
$Multimodel \ optimization \ {}_{\rm (New)}$	Mixture of Gaussians		3.2
Deep-Learning Algorithms			
Stochastic Gradient Descent	Gaussian (fixed cov.)	Delta approx., Stochastic approx.	4.1
$\operatorname{RMSprop}/\operatorname{Adam}$	Gaussian (diagonal cov.)	Delta approx., Stochastic approx.,	4.2,
		Hessian approx., Square-root scaling, Slow-moving scale vectors	4.3
Dropout	Mixture of Gaussians	Delta approx., Stochastic approx., Responsibility approx.	4.4
STE	Bernoulli	Delta approx., Stochastic approx.	4.6
Online Gauss-Newton (OGN) (New)	Gaussian (diagonal cov.)	Gauss-Newton Hessian approx. in Adam & no square-root scaling	4.5
Variational OGN (New)	"	Remove Delta approx. from OGN	4.5
Bayesian Binary NN (New)	((	Remove Delta approx. from STE	4.6
Approximate Bayesian Inference Algorithms			
Conjugate Bayes	Exp-family	Set learning rate $\rho_t = 1$	5.1
Laplace's method	Gaussian	Delta approx.	5.2
Expectation-Maximization	Exp-Family + Gaussian	Delta approx. for the parameters	5.3
Stochastic VI (SVI)	Exp-family (mean-field)	Stochastic approx., local rate $\rho_t = 1$	5.4
VMP	(	Set learning rate $\rho_t = 1$	5.4
Non-Conjugate VMP	(		5.4
Non-Conjugate VI (New)	Mixture of Exp-family	None	5.5

#### Khan and Rue. "Learning-Algorithms from Bayesian Principles" (2020)

Work in progress (draft available at https:// emtiyaz.github.io/papers/ learning\_from\_bayes.pdf)

We can compute uncertainty using a variant of Adam.

Khan, et al. "Fast and scalable Bayesian deep learning by weight-perturbation in Adam." *ICML* (2018).
Osawa et al. "Practical Deep Learning with Bayesian Principles." NeurIPS (2019).

# **Uncertainty of Deep Nets**

### VOGN: A modification of Adam but match the performance on ImageNet



Code available at <a href="https://github.com/team-approx-bayes/dl-with-bayes">https://github.com/team-approx-bayes/dl-with-bayes</a>

Khan, et al. "Fast and scalable Bayesian deep learning by weight-perturbation in Adam." *ICML* (2018).
Osawa et al. "Practical Deep Learning with Bayesian Principles." NeurIPS (2019).



#### Image Segmentation

Uncertainty (entropy of class probs)

(By Roman Bachmann)<sup>17</sup>

#### Learning-Algorithms from Bayesian Principles

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#### Abstract

We show that many machine-learning algorithms are specific instances of a *single* algorithm called the Bayesian learning rule. The rule, derived from Bayesian principles, yields a wide-range of algorithms from fields such as optimization, deep learning, and graphical models. This includes classical algorithms such as ridge regression, Newton's method, and Kalman filter, as well as modern deep-learning algorithms such as stochastic-gradient descent, RMSprop, Adam, and Dropout. The key idea is to estimate posterior approximations using the Bayesian learning rule. Different approximations then result in different algorithms and further algorithmic approximations give rise to variants of those algorithms. Our work shows that Bayesian principles not only unify, generalize, and improve existing learning-algorithms, but also help us design new ones.

#### Available at

https://emtiyaz.github.io/papers/learning\_from\_bayes.pdf



Human Learning at the age of 6 months.

NEURAL INFORMATION PROCESSING SYSTEMS

### Deep Learning with Bayesian Principles

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by Mohammad Emtiyaz Khan · Dec 9, 2019

### NeurIPS 2019 Tutorial



by Mohammad Emtivaz Khan

8,084 views · Dec 9, 2019

Efficient Processing of Deep Neural Network: from Algorithms to...

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# **Relevance of Data Examples**

Which examples are most relevant for the classifier? Red circle vs Blue circle.



# Model view vs Data view

Bayes "automatically" defines data-relevance



# **Bayes Duality**

 Gaussian approx fom Bayes learning rule turn NN into Linear models & Gaussian Process (GPs) [1].

$$\sum_{i=1}^{N} \ell(y_i, f_{\theta}(x_i)) \approx \sum_{i=1}^{N} \frac{1}{\sigma_i^2} [\tilde{y}_i - \phi_i(x_i)^{\top} \theta]^2$$
  
neural network

"Dual" variables obtained from  $\nabla_{\mu} \mathbb{E}_q[\ell_i(\theta)]$ (For Gaussian approx, obtained from Jacobian, residual etc.)

- $\sigma_i^2$  define the "relevance" of the data examples. We call more relevant ones the "memorable examples".
- Natural-gradients give "dual variables" (Bayes Duality)

1. Khan et al. "Approximate Inference Turns Deep Networks into Gaussian Processes." *NeurIPS* (2019).





# Life-Long Learning with Bayes



Kirkpatrick, James, et al. "Overcoming catastrophic forgetting in neural networks." PNAS 2017
Pan et al. Continual Deep Learning by Functional Regularisation of Memorable Past, NeurIPS, 2020

### Functional Regularization of Memorable Past (FROMP)

Regularize the function outputs. Simply adds an additional term in Adam.



1. Pan et al. Continual Deep Learning by Functional Regularisation of Memorable Past, NeurIPS, 2020

# Bayes is indispensable for an AI that learns as efficiently as we do



## How to design AI that learn like us?

- Uncertainty -> Learning -> Knowledge
- Three questions
  - Q1: What do we know? (model)
  - Q2: What do we not know? (uncertainty)
  - Q3: What do we need to know? (action & exploration)
- Posterior approximation is the key
  - (Q1) Models == representation of the world
  - (Q2) Posterior approximations == representation of the model
  - (Q3) The Bayes-dual representation will enable
    - represent learned knowledge,
    - reuse them in novel situations,
    - interact with the environment to collect new knowledge

#### Gaussian-Process-Based Emulators for Building Performance Simulation

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<sup>1</sup>Interdisciplinary Laboratory of Performance-Integrated Design (LIPID), Ecole Polytechnique Federale de Lausanne (EPFL), Switzerland.
<sup>2</sup>RIKEN Center for Advanced Intelligence Project, Tokyo, Japan.

#### Nonlinear models work extremely well

#### Abstract

In this paper, we present an emulator of a buildingenergy performance simulator. Previous work on emulators for this application has largely focused on linear models. Since the simulator itself is a collection of differential equations, we expect non-linear models to be better emulators than linear models. The emulator we present in this paper is based on Gaussian-process (GP) regression models. We show that the proposed non-linear model is 3-4 times more accurate than linear models in predicting the energy outputs of the simulator. For energy outputs in the range 10-800 kWh/m<sup>2</sup>, our model achieves an average error of 10-25 kWh/m<sup>2</sup> compared to an average error of 30-100 kWh/m<sup>2</sup> from using linear models. In addition to being very accurate, our emulator also heavily reduces the computational burden for building designers who rely on simulators. By providing performance feedback for building designs very quickly (in just a few milliseconds), we expect our approach to be particularly useful for exercises that involve a large number of simulations, e.g., Uncertainty Analysis (UA), Sensitivity Analysis (SA), robust design, and optimisa-



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## **Approximate Bayesian Inference Team**



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https://team-approxbayes.github.io/

We have openings for "parttime" student positions and also a postdoc/tech-staff position.



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